# Chapter 6.1.3 

## SHELXL-97

## Examples

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## 3. Examples of Small Molecule Refinements with SHELXL

Two test structures supplied with the SHELXL-97 are intended to provide a good illustration of routine small moiety structure refinement. The output discussed here should not differ significantly from that of the test jobs, except that it has been abbreviated and there may be differences in the last decimal place caused by rounding errors.

### 3.1 First example (ags4)



The first example (provided as the files ags4.ins and ags4.hkl) is the final refinement job for the polymeric inorganic structure $\mathrm{Ag}(\mathrm{NCSSSSCN})_{2} \mathrm{AsF}_{6}$, determined by Roesky, Gries, Schimkowiak \& Jones (1986). Each ligand bridges two $\mathrm{Ag}^{+}$ions so each silver is tetrahedrally coordinated by four nitrogen atoms. The silver, arsenic and one of the fluorine atoms lie on special positions. Normally the four unique heavy atoms (from Patterson interpretation using SHELXS) would have been refined isotropically first and the remaining atoms found in a difference synthesis, and possibly an intermediate job would have been performed with the heavy atoms anisotropic and the light atoms isotropic. For test purposes we shall simply input the atomic coordinates which assumes isotropic U's of 0.05 for all atoms. In this job all atoms are to be made anisotropic (ANIS). We shall further assume that a previous job has recommended the weighting scheme used here (WGHT) and shown that one reflection is to be suppressed in the refinement because it is clearly erroneous (OMIT).

The first 9 instructions (TITL...UNIT) are the same for any SHELXS and SHELXL job for this structure and define the cell dimensions, symmetry and contents. The SHELXTL program XPREP can be used to generate these instructions automatically
for any space group etc. SHELXL knows the scattering factors for the first 94 neutral atoms in the Periodic Table. Ten least-squares cycles are to be performed, and the ACTA instruction ensures that the CIF files ags4.cif and ags4.fcf will be written for archiving and publication purposes. ACTA also sets up the calculation of bond lengths and angles (BOND) and a final difference electron density synthesis (FMAP 2) with peak search (PLAN 20). The HKLF 4 instruction terminates the file and initiates the reading of the ags4.hkl intensity data file.

It is possible to set up special position constraints on the $x, y, z$-coordinates, occupation factors, and $\mathrm{U}_{\mathrm{ij}}$ components by hand. However this is totally unnecessary because the program will do this automatically for any special position in any space group, conventional or otherwise. Similarly the program recognizes polar space groups ( $\mathrm{P} \overline{4}$ is non-polar) and applies appropriate restraints (Flack \& Schwarzenbach, 1988), so it is no longer necessary to worry about fixing one or more coordinates to prevent the structure drifting along polar axes. It is not necessary to set the overall scale factor using an FVAR instruction for this initial job, because the program will itself estimate a suitable starting value. Comments may be included in the .ins file either as REM instructions or as the rest of a line following '!'; this latter facility has been used to annotate this example.

```
TITL AGS4 in P-4 ! title of up to 76 characters
CELL 0.71073 8.381 8.381 6.661 90 90 90 ! wavelength and unit-cell
ZERR 1 .002 .002 .001 0 0 0 ! Z (formula-units/cell), cell
esd's
LATT -1 ! non-centrosymmetric primitive
lattice
SYMM -X, -Y, Z
SYMM Y, -X, -Z ! symmetry operators (x,y,z must be left out)
SYMM -Y, X, -Z
SFAC C AG AS F N S ! define scattering factor numbers
UNIT 4 1 1 6 4 8 ! unit cell contents in same order
L.S. 10
ACTA
OMIT -2 3 1
ANIS ! convert all (non-H) atoms to anisotropic
WGHT 0.037 0.31
    ! weighting scheme
\begin{tabular}{lllll} 
AG & 2 & .000 & .000 & .000 \\
AS & 3 & .500 & .500 & .000
\end{tabular}
S1 6 . 368 . 206 . 517 ! atom name, SFAC number, x, y, z (usually
S2 6 . 386 .034 . 736 ! followed by sof and U(iso) or Uij); the
C 1 . 278 .095 . 337 ! program automatically generates special
N 5 . 211 .030 . 214 ! position constraints
F1 4 . 596 . 325 -. 007
F2 4 . 500 . 500 . }24
HKLF 4
! read h,k,1,Fo^2,sigma(FO^2) from 'ags4.hkl'
```

The . Ist listing file starts with a header followed by an echo of the above .ins file. After reading TITL...UNIT the program calculates the cell volume, $F(000)$, absorption coefficient, cell weight and density. If the density is unreasonable, perhaps the unit-cell contents have been given incorrectly. The next items in the
.Ist file are the connectivity table and the symmetry operations used to include a shell of symmetry equivalent atoms (so that all unique bond lengths and angles can be found):

```
Covalent radii and connectivity table for AGS4 in P-4
C 0.770
AG 1.440
AS 1.210
F 0.640
N 0.700
S 1.030
Ag - N N_$3 N_$4 N_$2
As - F2 F2_$6 F1_$7 F1_$6 F1_$5 F1
S1 - C S2
S2 - S2_$1 S1
C - N S1
N - C Ag
F1 - As
F2 - As
Operators for generating equivalent atoms:
$1 -x+1, -y+1, z
$2 -x, -y, z
$3 y, -x, -z
$4 -y, x, -z
$5 -x+1, -y+1, z
$6 y, -x+1, -z
$7 -y+1, x, -z
```

Note that in addition to symmetry operations generated by the program, one can also define operations with the EQIV instruction and then refer to the corresponding atoms with $\_\mathrm{n}$ in the same way. Thus:

```
EQIV $1 1-x, -y, z
CONF S1 S2 S2_$1 S1_$1
```

could have been included in ags4.ins to calculate the S-S-S-S torsion angle. If EQIV instructions are used, the program renumbers the other symmetry operators accordingly.

The next part of the output is concerned with the data reduction:

```
    1475 Reflections read, of which 1 rejected
0 =< h =< 10, -9 =< k =< 10, 0 =< l =< 8, Max. 2-theta =
55.00
    O Systematic absence violations
Inconsistent equivalents etc.
```



Special position constraints are then generated and the statistics from the first least-squares cycle are listed (the output has been compacted to fit the page). The maximum vector length refers to the number of reflections processed simultaneously in the rate-determining calculations; usually the program utilizes all available memory to make this as large as possible, subject to a maximum of 511. This maximum may be reduced (but not increased) by means of the fourth parameter on the L.S. (or CGLS) instruction; this may be required to prevent unnecessary disk transfers when large structures are refined on virtual memory systems with limited physical memory. The number of parameters refined in the current cycle is followed by the total number of refinable parameters (here both are 55).

```
Special position constraints for Ag
x=0.0000 y= y m = 0000 U22 = 1.0 * U11
U23 = 0 U13 = 0 U12 = 0 sof = 0.25000
Special position constraints for As
x=0.5000 y = 0.5000 z = 0.0000 U22 = 1.0 * U11
U23 = 0 U13 = 0 U12 = 0 sof = 0.25000
Special position constraints for F2
x = 0.5000 y = 0.5000 U23 = 0 U13 = 0
sof = 0.50000
```




Only the largest shift/esd's are printed. More output could have been obtained using 'MORE 2' or 'MORE 3'. The largest correlation matrix elements are printed after the last cycle, in which the mean and maximum shift/esd have been reduced to 0.003 and 0.017 respectively. This is followed by the full table of refined coordinates and $\mathrm{U}_{\mathrm{ij}}$ 's with esd's (too large to include here, but similar to the corresponding table in SHELX-76 except that $U_{\text {eq }}$ and its esd are also printed) and by a final structure factor calculation:

```
Final Structure Factor Calculation for AGS4 in P-4
Total number of l.s. parameters = 55 Maximum vector length = 511
wR2 = 0.0780 before cycle 11 for 903 data and 2 / 55 parameters
GooF = S = 1.063; Restrained GooF = 1.063 for 0
restraints
Weight = 1/[sigma^2 (FO^2)+(0.0370*P)^2+0.31*P] where
P=(Max (FO^2,0)+2*Fc^2)/3
R1 = 0.0322 for 818 Fo > 4.sigma(Fo) and 0.0367 for all 903 data
wR2 = 0.0780, GooF = S = 1.063, Restrained GooF = 1.063 for all
data
Flack x parameter = 0.0224 with esd 0.0260 (expected values are 0
(within 3 esd's) for correct and +1 for inverted absolute structure)
```

There are some important points to note here. The weighted $R$-index based on $F_{0}{ }^{2}$ is (for compelling statistical reasons) much higher than the conventional $R$-index based on $F_{0}$ with a threshold of say $F_{0}>4 \sigma\left(F_{0}\right)$. For comparison with structures refined against $F$ the latter is therefore printed as well (as $R 1$ ). Despite the fact that $w R 2$ and not $R 1$ is the quantity minimized, $R 1$ has the advantage that it is relatively insensitive to the weighting scheme, and so is more difficult to manipulate.

Since the structure is non-centrosymmetric, the program has automatically estimated the Flack absolute structure parameter $x$ in the final structure factor summation. In this example $x$ is within one esd of zero, and its esd is also relatively small. This provides strong evidence that the absolute structure has been assigned correctly, so that no further action is required. The program would have printed a warning here if it would have been necessary to 'invert' the structure or to refine it as a racemic twin.

This is followed by a list of principal mean square displacements $U$ for all anisotropic atoms. It will be seen that none of the smallest components (in the third column) are in danger of going negative [which would make the atom 'non
positive definite' (NPD)] but that the motion of the two unique fluorine atoms is highly anisotropic (not unusual for an $\mathrm{AsF}_{6}$ anion). The program suggests that the fluorine motion is so extended in one direction that it would be possible to represent each of the two fluorine atoms as disordered over two sites, for which $x$, $y$ and $z$ coordinates are given; this may safely be ignored here (although there may well be some truth in it). The two suggested new positions for each 'split' atom are placed equidistant from the current position along the direction (and reverse direction) corresponding to the largest eigenvalue of the anisotropic displacement tensor.

This list is followed by the analysis of variance (reproduced here in squashed form), recommended weighting scheme (to give a flat analysis of variance in terms of $F_{\mathrm{c}}{ }^{2}$ ), and a list of the most disagreeable reflections. For a discussion of the analysis of variance see the second example.


```
Analysis of variance for reflections employed in refinement
K = Mean[FO^2] / Mean[FC^2] for group
Fc/Fc(max) 0.000 0.026 0.039 0.051 0.063 0.082 0.103 0.147 0.202 0.306
1.0
Number in group 94. 89. 90. 91. 89. 91. 89. 91. 88.
91.
GooF 1.096 1.101 0.997 1.078 1.187 1.069 1.173 0.922 1.019 0.966
K
                                1.560 1.053 1.010 1.004 1.007 1.021 1.026 1.002 0.997 0.984
```



```
inf
Number in group 97. 84. 92. 91. 89. 90. 89. 90. 93.
88.
GooF 1.067 0.959 0.935 0.895 1.035 1.040 1. 115 1.149 1.161 1.228
K 1.047 1.010 1.009 0.991 1.004 0.996 0.989 1.012 0.997 0.982
R1 0.166 0.100 0.069 0.059 0.051 0.036 0.033 0.027 0.020 0.020
Recommended weighting scheme: WGHT 0.0314 0.3674
```

Most Disagreeable Reflections (* if suppressed or used for Rfree)

| h | k | 1 | FO^2 |  | $\mathrm{Fc}^{\wedge} 2$ | Delta (F^2) /esd | Fc/F (max) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Resolution (A) |  |  |  |  |  |  |  |
| 4 | 4 | 4 | 18.32 | 33.30 | 3.62 | 0.062 | 1.11 |
| -4 | 1 | 3 | 15.79 | 4.17 | 3.50 | 0.022 | 1.50 |
| 0 | 2 | 2 | 41.60 | 57.32 | 3.26 | 0.082 | 2.61 |

After the table of bond lengths and angles (BOND was implied by the ACTA instruction), the data are merged (again) for the Fourier calculation after correcting for dispersion (because the electron density is real). In contrast to the initial data reduction, Friedel's law is assumed here; the aim is to set up a unique reflection list so that the (difference) electron density can be calculated on an absolute scale.

The algorithm for generating the 'asymmetric unit' for the Fourier calculations is general for all space groups, in conventional settings or otherwise. The rms electron density (averaged over all grid points) is printed as well as the maximum and minimum values so that the significance of the latter can be assessed. Since PLAN 20 was assumed, only a peak list is printed (and written to the .res file), followed by a list of shortest distances between peaks (not shown below); PLAN -20 would have produced a more detailed analysis with 'printer plots' of the structure. The last 40 peaks and some of the interatomic distances have been deleted here to save space. In this table, 'distances to nearest atoms' takes symmetry equivalents into account.

```
Bond lengths and angles
    [severely squashed to fit page!]
Ag - Distance Angles
N 2.2788(0.0058)
N_$2 2.2788(0.0058) 113.08(0.15)
N_$4 2.2788(0.0058) 113.08(0.15) 102.47(0.29)
N_$3 2.2788(0.0058) 102.47(0.29) 113.08(0.15) 113.08(0.15)
    Ag - N N_$3 N_$4
As - Distance Angles
F2 1.6399(0.007)
F2_$6 1.6399(0.007)180.00(0.00)
F1_$7 1.6724(0.0037) 89.08(0.41) 90.92(0.41)
F1_$6 1.6724(0.0037) 89.08(0.41) 90.92(0.41)178.15(0.82)
F1_$5 1.6724(0.0037) 90.92(0.41) 89.08(0.41) 90.01(0.01) 90.01(0.01)
F1 1.6724(0.0037) 90.92(0.41) 89.08(0.41) 90.01(0.01)
90.01(0.01)178.15(0.82)
    As - F2 F2_$6 F1_$7 F1_$6 F1_$5
S1 - Distance Angles
C 1.6819(0.0069)
S2 2.0633(0.0025) 98.61(0.20)
            S1 - C
S2 - Distance Angles
S2_$1 2.0114(0.0028)
S1 2.0633(0.0025) 105.37(0.07)
```

| S2 - S2_\$1 |  |  |
| :---: | :---: | :---: |
| C - Distance Angles |  |  |
| N 1.1472 (0.0074) |  |  |
| S1 | $1.6819(0.0069)$ | 175.67(0.49) |
|  | C - | N |
| N - Distance Angles |  |  |
| C 1.1472 (0.0074) |  |  |
| Ag | 2.2788 (0.0058) | 152.38(0.45) |
|  | N - | C |
| F1 - Distance Angles |  |  |
| As 1.6724(0.0037) |  |  |
| F1 - |  |  |
| F2 - Distance Angles |  |  |
| As 1.6399(0.0075) |  |  |
| F2 - |  |  |

FMAP and GRID set by program

FMAP 2318
GRID $-3.333-2 \quad-1 \quad 3.333 \quad 2 \quad 1$

R1 $=0.0370$ for 590 unique reflections after merging for Fourier

Electron density synthesis with coefficients Fo-Fc
Highest peak 0.32 at 0.0000 0.0000 $0.5000 \quad[2.60$ A from N]
Deepest hole -0.36 at 0.5000 0.5000 0.1863 [0.40 A from F2]
Mean $=0.00$, Rms deviation from mean $=0.07$
$1133 / 13851$

Fourier peaks appended to .res file

|  |  | $\mathbf{x}$ | Y | z | sof | U | Peak | Dist t |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q1 | 1 | 0.0000 | 0.0000 | 0.5000 | 0.25000 | 0.05 | 0.32 | 2.60 N | 2.69 C | 3.33 AG |
| Q2 | 1 | 0.5690 | 0.3728 | 0.1623 | 1.00000 | 0.05 | 0.27 | 1.20 F1 | 1.34 F 2 | 1.62 AS |
| Q3 | 1 | 0.5685 | 0.3851 | -0 | 1.000 | 0. | 0.24 | 1.19 F 1 | 1.25 F 2 | 1.56 AS |
| Q4 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0.81 F 2 | 1.78 AS | 1.79 |
| Q5 | 1 | 0.5848 | 0.2667 | 0.0312 | 1.00000 | 0.05 | 0.23 | 0.55 F 1 | 2.09 AS | 2.47 F1 |
| Q6 | 1 | 0.5495 | 0.3425 | -0.1122 | 1.00000 | 0.05 | 0.21 | 0.83 F 1 | 1.57 AS | 1.65 F 2 |
| Q7 | 1 | 0.2617 | -0.1441 | 0.1446 | 1.00000 | 0.05 | 0.20 | 1.59 N | 2.17 F1 | 2.40 C |
| Q8 | 1 | 0.7221 | 0.1898 | 0.0030 | 1.00000 | 0.05 | 0.20 | 1.55 F1 | 2.39 N | 2.54 N |
| Q9 | 1 | 0.1997 | 0.0293 | 0.1024 | 1.00000 | 0.05 | 0.19 | 0.75 N | 1.79 C | 1.82 AG |
| Q10 | 1 | 0.4606 | -0.0113 | 0.8165 | 1.00000 | 0.05 | 0.19 | 0.91 S 2 | 1.41 S 2 | 2.82 S 1 |

### 3.2 Second example (sigi)



In the second example (provided as the files sigi.ins and sigi.hkl) a small organic structure is refined in the space group $\mathrm{P} \overline{1}$. Only the features that are different from the ags 4 refinement will be discussed in detail. The structure consists of a five-membered lactone [-C7-C11-C8-C4(O1)-O3-] with a - $\mathrm{CH}_{2}-\mathrm{OH}$ group [-C5-O2] attached to C 7 and $\mathrm{a}=\mathrm{C}\left(\mathrm{CH}_{3}\right)\left(\mathrm{NH}_{2}\right)$ unit $[=\mathrm{C} 9(\mathrm{C} 10) \mathrm{N} 6]$ double-bonded to C 8 .

Of particular interest here is the placing and refinement of the 11 hydrogen atoms via HFIX instructions. The two $-\mathrm{CH}_{2}-$ groups ( C 5 and C 11 ) and one tertiary CH (C7) can be placed geometrically by standard methods; the algorithms have been improved relative to those used in SHELX-76, and the hydrogen atoms are now idealized before each refinement cycle (and after the last). Since N6 is attached to a conjugated system, it is reasonable to assume that the $-\mathrm{NH}_{2}$ group is coplanar with the C8=C9(C10)-N6 unit, which enables these two hydrogens to be placed as ethylenic hydrogens, requiring HFIX (or AFIX) 9n; the program takes into account that they are bonded to nitrogen in setting the default bond lengths. All these hydrogens are to be refined using a 'riding model' (HFIX or AFIX m3) for $x$, $y$ and $z$.

The -OH and $-\mathrm{CH}_{3}$ groups are trickier, in the latter case because C 9 is $\mathrm{sp}^{2}$ hybridized, so the potential barrier to rotation is low and there is no fully staggered conformation available as the obvious choice. Since the data are reasonable, the initial torsion angles for these two groups can be found by means of difference electron density syntheses calculated around the circles which represent the loci of all possible hydrogen atom positions. The torsion angles are then refined during the least-squares refinement. Note that in subsequent cycles (and jobs) these groups will be re-idealized geometrically with retention of the current torsion angle; the circular Fourier calculation is performed only once. Two 'free variables' (2 and 3 yes, they still exist!) have been assigned to refine common isotropic displacement parameters for the 'rigid' and 'rotating' hydrogens respectively. If these had not been specified, the default action would have been
to hold the hydrogen $U$ values at 1.2 times the equivalent isotropic $U$ of the atoms to which they are attached ( 1.5 for the -OH and methyl groups).

The sigi.ins file (which is provided as a test job) is as follows. Note that for instructions with both numerical parameters and atom names such as HFIX and MPLA, it does not matter whether numbers or atoms come first, but the order of the numerical parameters themselves (and in some cases the order of the atoms) is important.

```
TITL SIGI in P-1
CELL 0.71073 6.652 7.758 8.147 73.09 75.99 68.40
ZERR 2 . 002 . 002 . 002 . 03 . 03 . 03
SFAC C H N O
UNIT 14 22 2 6 ! no LATT and SYMM needed for space group P-1
L.S. 4
EXTI 0.001 ! refine an isotropic extinction parameter
WGHT .060 0.15 ! (suggested by program in last job); WGHT
OMIT 2 8 0 ! and OMIT are also based on previous output
BOND $H ! include H in bond lengths / angles table
CONF ! all torsion angles except involving hydrogen
HTAB ! analyse all hydrogen bonds
FMAP 2 ! Fo-FC Fourier
PLAN -20 ! printer plots and full analysis of peak list
HFIX 147 31 O2 ! initial location of -OH and -CH3 hydrogens from
HFIX 137 31 C10 ! circular Fourier, then refine torsion, U(H)=fv(3)
HFIX 93 21 N6 ! -NH2 in plane, xyz ride on N, U(H)=fv(2)
HFIX 23 21 C5 C11 ! two -CH2- groups, xyz ride on C, U(H)=fv(2)
HFIX 13 21 C7 ! tertiary CH, xyz ride on C, U(H)=fv(2)
EQIV $1 X-1, Y, Z ! define symmetry operations for H-bonds
EQIV $2 X+1, Y, Z-1
HTAB N6 O1 ! outputs H-bonds D-H...A with esds
HTAB O2 O1_$1 ! _$1 and _$2 refer to symmetry equivalents
HTAB N6 O2_$2
through
MPLA 5 C7 C11 C8 C4 O3 O1 N6 C9 C10 ! CNC=CCC moiety, then find deviations
MPLA 6 C10 N6 C9 C8 C11 C4 O1 O3 C7 ! of last 4 and 3 named atoms resp. too
FVAR 1 .06 .07 ! overall scale and free variables for
U(H)
REM name sfac# x y z sof(+10 to fix it) U11 U22 U33 U23 U13 U12 follow
01 4 0.30280 0.17175 0.68006 11.00000 0.02309 0.04802 =
    0.02540 -0.00301 -0.00597 -0.01547
02 4 -0.56871 0.23631 0.96089 11.00000 0.02632 0.04923 =
    0.02191 -0.00958 0.00050 -0.02065
03 4 -0.02274 0.28312 0.83591 11.00000 0.02678 0.04990 =
    0.01752 -0.00941 -0.00047 -0.02109
C4 1 0.10358 0.23458 0.68664 11.00000 0.02228 0.02952 =
        0.01954 -0.00265 -0.00173 -0.01474
C5 1 -0.33881 0.18268 0.94464 11.00000 0.02618 0.03480 =
    0.01926 -0.00311 -0.00414 -0.01624
N6 3 0.26405 0.17085 0.33925 11.00000 0.03003 0.04232 =
    0.02620 -0.01312 0.00048 -0.01086
```

```
C7 1 -0.25299 0.33872 0.82228 11.00000 0.02437 0.03111 =
    0.01918 -0.00828 -0.00051 -0.01299
C8 1 -0.03073 0.27219 0.55976 11.00000 0.02166 0.02647 =
    0.01918 -0.00365 -0.00321 -0.01184
C9 1 0.05119 0.24371 0.39501 11.00000 0.02616 0.02399 =
    0.02250 -0.00536 -0.00311 -0.01185
C10 1 -0.10011 0.29447 0.26687 11.00000 0.03877 0.04903 =
    0.02076 -0.01022 -0.00611 -0.01800
C11 1 -0.26553 0.36133 0.63125 11.00000 0.02313 0.03520 =
    0.01862 -0.00372 -0.00330 -0.01185
```

HKLF 4 ! read intensity data from 'sigi.hkl'; terminates '.ins' file
END

The data reduction reports 1904 reflections read (one of which was rejected by OMIT) with indices $-7 \leq h \leq 7,-8 \leq k \leq 9$ and $-9 \leq l \leq 9$. Note that these are the limiting index values; in fact only about 1.5 times the unique volume of reciprocal space was measured. The maximum $2 \theta$ was 50.00 , and there were no systematic absence violations, 34 (not seriously) inconsistent equivalents, and 1296 unique data. $R$ (int) was 0.0196 and $R($ sigma) 0.0151 .

The program uses different default distances to hydrogen for different bonding situations; these may be overridden by the user if desired. These defaults depend on the temperature (set using TEMP) in order to allow for librational effects. The list of default X-H distances is followed by the (squashed) circular difference electron density syntheses to determine the $\mathrm{C}-\mathrm{OH}$ and $\mathrm{C}-\mathrm{CH}_{3}$ initial torsion angles:

```
Default effective X-H distances for T = 20.0 C
AFIX m = 1 2 2 3 4 4 4 [N] 3[N] 15[B] 8[O] 9 9[N] 16
```



```
Difference electron density (eA^-3x100) at 15 degree intervals for AFIX 147
group attached to 02. The center of the range is eclipsed (cis) to C7 and
rotation is clockwise looking down C5 to O2
    2 -2 -6 -9 - - - -5 -1 0 0 0 0 0 1 0 0 -2 -2 0
Difference electron density (eA^-3x100) at 15 degree intervals for AFIX 137
group attached to C10. The center of the range is eclipsed (cis) to N6 and
rotation is clockwise looking down C9 to C10
    50}44
After local symmetry averaging: }\begin{array}{lllllllll}{40}&{41}&{36}&{28}&{21}&{20}&{24}&{33}
```

It will be seen that the hydroxyl hydrogen is very clearly defined, but that the methyl group is rotating fairly freely (low potential barrier). After three-fold averaging, however, there is a single difference electron density maximum. The (squashed) least-squares refinement output follows:


| H5A | -0.2721 | 0.0676 | 0.9001 | 23 | 0.970 | 0.000 | C5 | O2 | C7 |  |
| :--- | ---: | ---: | :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- |
| H5B | -0.2964 | 0.1554 | 1.0576 | 23 | 0.970 | 0.000 | C5 | O2 | C7 |  |
| H6A | 0.3572 | 0.1389 | 0.4085 | 93 | 0.860 | 0.000 | N6 | C9 | C8 |  |
| H6B | 0.3073 | 0.1559 | 0.2347 | 93 | 0.860 | 0.000 | N6 | C9 | C8 |  |
| H7 | -0.3331 | 0.4598 | 0.8575 | 13 | 0.980 | 0.000 | C7 | O3 | C5 | C11 |
| H10A | -0.0176 | 0.2947 | 0.1525 | 137 | 0.960 | 0.000 | C10 | C9 | H10A |  |
| H10B | -0.2042 | 0.4192 | 0.2692 | 137 | 0.960 | 0.000 | C10 | C9 | H10A |  |
| H10C | -0.1764 | 0.2036 | 0.2964 | 137 | 0.960 | 0.000 | C10 | C9 | H10A |  |
| H11A | -0.3575 | 0.2948 | 0.6198 | 23 | 0.970 | 0.000 | C11 | C8 | C7 |  |
| H11B -0.3198 | 0.4943 | 0.5737 | 23 | 0.970 | 0.000 | C11 | C8 | C7 |  |  |

The final structure factor calculation, analysis of variance etc. produces the following edited output:

```
Final Structure Factor Calculation for SIGI in P-1
Total number of l.s. parameters = 105 Maximum vector length = 511
wR2 = 0.1035 before cycle 5 for 1296 data and 0 / 105 parameters
GooF = S = 1.016; Restrained GooF = 1.016 for 0 restraints
Weight = 1/[sigma^2 (Fo^2)+(0.0600*P)^2+0.15*P] where
P=(Max (Fo^2,0) +2*Fc^2)/3
R1 = 0.0364 for 1189 Fo > 4.sigma(Fo) and 0.0397 for all 1296 data
wR2 = 0.1035, GooF = S = 1.016, Restrained GooF = 1.016 for all data
Occupancy sum of asymmetric unit = 11.00 for non-hydrogen and 11.00 for
hydrogen atoms.
```

Principal mean square atomic displacements $U$

| 0.0504 | 0.0254 | 0.0188 | O1 |
| :--- | :--- | :--- | :--- |
| 0.0492 | 0.0229 | 0.0189 | O2 |
| 0.0513 | 0.0194 | 0.0165 | 03 |
| 0.0326 | 0.0208 | 0.0159 | C4 |
| 0.0376 | 0.0204 | 0.0190 | C5 |
| 0.0439 | 0.0319 | 0.0214 | N6 |
| 0.0329 | 0.0201 | 0.0185 | C7 |
| 0.0276 | 0.0190 | 0.0181 | C8 |
| 0.0289 | 0.0220 | 0.0191 | C9 |
| 0.0493 | 0.0352 | 0.0181 | C10 |
| 0.0353 | 0.0215 | 0.0183 | C11 |

Analysis of variance for reflections employed in refinement $\mathrm{K}=$ Mean $\left[\mathrm{FO}^{\wedge} 2\right] /$ Mean [ $\left.\mathrm{FC}^{\wedge} 2\right]$ for group
$\begin{array}{llllllllllllllllll}\text { FC/FC (max) } & 0.000 & 0.009 & 0.017 & 0.027 & 0.038 & 0.049 & 0.065 & 0.084 & 0.110 & 0.156 & 1.0\end{array}$

Number in group 135. 125. 131. 139. 119. 132. 131. 128. 131. 126. GooF $1.0341 .0001 .0851 .0461 .0930 .999 \quad 0.9370 .9951 .0270 .931$
$\begin{array}{lllllllllllllllll}\mathrm{K} & 1.567 & 1.127 & 0.964 & 1.023 & 1.008 & 0.992 & 0.997 & 0.998 & 1.008 & 1.010\end{array}$
$\begin{array}{llllllllllll}\text { Resolution(A) } & 0.84 & 0.88 & 0.90 & 0.95 & 0.99 & 1.06 & 1.14 & 1.25 & 1.44 & 1.79 & \text { inf }\end{array}$

Number in group 136. 127. 128. 128. 136. 124. 128. 130. 130. 129. GooF $0.9780 .8810 .854 \quad 0.850 \quad 0.850 \quad 0.921 \quad 0.8741 .088 \quad 1.2421 .434$
$\begin{array}{lllllllllllllll}\mathrm{K} & 1.024 & 1.013 & 1.017 & 0.990 & 0.991 & 0.989 & 1.013 & 0.995 & 1.037 & 1.004\end{array}$
$\begin{array}{lllllllllllllllllllll}\text { R1 } \quad 0.061 & 0.049 & 0.050 & 0.046 & 0.034 & 0.034 & 0.031 & 0.039 & 0.037\end{array}$

Recommended weighting scheme: WGHT 0.05450 .1549
The analysis of variance should be examined carefully for indications of systematic errors. If the Goodness of Fit (GooF) is significantly higher than unity and the scale factor K is appreciably lower than unity in the extreme right columns in terms of both $F$ and resolution, then an extinction parameter should be refined (the program prints a warning in such a case). This does not show here because an extinction parameter is already being refined. The scale factor is a little high for the weakest reflections in this example; this may well be a statistical artifact and may be ignored (selecting the groups on $F_{c}$ will tend to make $F_{o}{ }^{2}$ greater than $F_{\mathrm{c}}{ }^{2}$ for this range). The increase in the GooF at low resolution (the 1.79 to infinity range) is caused in part by systematic errors in the model such as the use of scattering factors based on spherical atoms which ignore bonding effects, and is normal for purely light-atom structures (this interpretation is confirmed by the fact that difference electron density peaks are found in the middle of bonds). In extreme cases the lowest or highest resolution ranges can be conveniently suppressed by means of the SHEL instruction; this is normal practice in macromolecular refinements, but refining a diffuse solvent model with SWAT may be better, inadequate solvent modeling for macromolecules produces similar symptoms to lack of extinction refinement for small molecules.

The weighting scheme suggested by the program is designed to produce a flat analysis of variance in terms of $F_{c}$, but makes no attempt to fit the resolution dependence of the GooF. It is also written to the end of the .res file, so that it is easy to update it before the next job. In the early stages of refinement it is better to retain the default scheme of WGHT 0.1; the updated parameters should not be incorporated in the next .ins file until all atoms have been found and at least the heavier atoms refined anisotropically.

The list of most disagreeable reflections and tables of bond lengths and angles (BOND \$H - omitted here) and torsion angles (CONF) are followed by the HTAB (hydrogen bonds) and MPLA (least-squares planes) tables:

```
Selected torsion angles
    -175.08 ( 0.12) C7 - O3 - C4 - O1
```

| 5.73 | ( 0.15) | C7- O3-C4-C8 |
| :---: | :---: | :---: |
| 109.69 | ( 0.12) | C4 - O3-C7- C5 |
| -11.65 | ( 0.15) | C4- O3-C7- C11 |
| 171.12 | ( 0.10) | O2-C5-C7-03 |
| -72.04 | ( 0.15) | O2-C5 - C7 - C11 |
| -1.46 | ( 0.24) | O1-C4-C8 - C9 |
| 177.61 | ( 0.12) | O3-C4 - C8 - C9 |
| -176.27 | ( 0.14) | O1-C4-C8 - C11 |
| 2.80 | ( 0.16) | O3-C4 - C8 - C11 |
| 3.08 | ( 0.22) | C4 - C8 - C9 - N6 |
| 176.93 | ( 0.13) | C11-C8 - C9 - N6 |
| -177.23 | ( 0.13) | C4 - C8 - C9 - C10 |
| -3.39 | ( 0.22) | C11-C8 - C9 - C10 |
| 176.05 | ( 0.13) | C9 - C8 - C11-C7 |
| -9.39 | ( 0.14) | C4 - C8 - C11 - C7 |
| 12.37 | ( 0.14) | O3-C7-C11-C8 |
| -104.74 | 0.13) | C5 - C7- C11 - C8 |

Specified hydrogen bonds (with esds except fixed and riding $H$ )

| D-H | H. .A | D. .A | $<($ DHA $)$ |  |
| :--- | :--- | :--- | :--- | :--- |
| 0.86 | 2.23 | $2.8486(18)$ | 129.3 | N6-H6A. .O1 |
| 0.82 | 2.04 | $2.8578(16)$ | 174.0 | O2-H2 . .O1_\$1 |
| 0.86 | 2.17 | $2.9741(19)$ | 155.1 | N6-H6B . .O2_\$2 |

```
Least-squares planes (x,y,z in crystal coordinates) and deviations from
them
    (* indicates atom used to define plane)
    2.3443 (0.0044) x + 7.4105 (0.0042) y - 0.0155 (0.0053) z = 1.9777
(0.0044)
* -0.0743 (0.0008) C7
* 0.0684 (0.0008) C11
* -0.0418 (0.0009) C8
* -0.0062 (0.0008) C4
    0.0538 (0.0008) 03
    -0.0061 (0.0020) 01
    -0.0980 (0.0028) N6
    -0.0562 (0.0023) C9
    -0.0314 (0.0030) C10
Rms deviation of fitted atoms = 0.0546
```

$2.5438(0.0040) x+7.3488(0.0040) y-0.1657(0.0042) z=1.8626$
(0.0026)
Angle to previous plane (with approximate esd) $=2.45$ ( 0.07 )

* 0.0054 (0.0008) C10
* $0.0082(0.0008)$ N6
* -0.0052 (0.0012) C9
* -0.0337 (0.0012) C8
* 0.0135 (0.0008) C11
* $0.0118(0.0009) \quad$ C4
0.0568 (0.0019) 01
0.0214 (0.0018) 03
$-0.1542(0.0020) \quad \mathrm{C7}$


All esds printed by the program are calculated rigorously from the full covariance matrix, except for the esd in the angle between two least-squares planes, which involves some approximations. The contributions to the esds in bond lengths, angles and torsion angles also take the errors in the unit-cell parameters (as input on the ZERR instruction) rigorously into account; an approximate treatment is used to obtain the (rather small) contributions of the cell errors to the esds involving least-squares planes.

There follows the difference electron density synthesis and line printer 'plot' of the structure and peaks. The highest and lowest features are 0.27 and $-0.17 \mathrm{eA}^{-3}$ respectively, and the rms difference electron density is 0.04 . These values confirm that the treatment of the hydrogen atoms was adequate, and are indeed typical for routine structure analysis of small organic molecules. This output is too voluminous to give here, and indeed users of the Siemens SHELXTL molecular graphics program XP will almost always suppress it by use of the default option of a positive number on the PLAN instruction, and employ interactive graphics instead for analysis of the peak list.

